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# Synthesis and characterization of the barium oxalates $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot \mathbf{0 . 5} \mathrm{H}_{2} \mathrm{O}, \alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ and $\beta-\mathrm{BaC}_{2} \mathrm{O}_{4}$ 

The synthesis of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ and its thermal decomposition to $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ and $\beta-\mathrm{BaC}_{2} \mathrm{O}_{4}$ was investigated. $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ is precipitated at room temperature from aqueous solutions of barium chloride and ammonium oxalate. The deuterated compound $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{D}_{2} \mathrm{O}$ was made in analogy with $\mathrm{D}_{2} \mathrm{O}$ as the solvent. The compounds were characterized by X-ray and neutron diffraction analysis. Single-crystal X-ray diffraction of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ measured at 120 K gave the triclinic cell $a=8.692$ (1), $b=9.216$ (1), $c=$ 6.146 (1) $\AA, \alpha=95.094$ (3), $\beta=95.492$ (3), $\gamma=64.500$ (3) ${ }^{\circ}$, space group $P \overline{1}, Z=4$. Two independent Ba atoms are each coordinated to nine O atoms at distances from 2.73 (1) to 2.99 (1) A. One of the two oxalate ions deviates significantly from planarity. The water molecule does form weak hydrogen bonds. In situ X-ray powder diffraction was used to study the thermal decomposition of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ and the formation of $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$. The X-ray powder pattern of $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ measured at 473 K was indexed on a triclinic cell with $a=$ 5.137 (3), $b=8.764$ (6), $c=9.006$ (4) $\AA, \alpha=83.57$ (4), $\beta=$ 98.68 (5), $\gamma=99.53$ (5) ${ }^{\circ}$, and the space group $P \overline{1}$ with $Z=4$.

## 1. Introduction

Barium oxalate forms four hydrates, of which hydrogen bonds have been studied of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 3 \cdot 5 \mathrm{D}_{2} \mathrm{O}$ (Neder et al., 1997), $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 2 \mathrm{D}_{2} \mathrm{O}$ (Christensen et al., 1995) and $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot \mathrm{D}_{2} \mathrm{O}$ (Christensen, 1992) by neutron powder diffraction analysis. The crystal structure of the barium oxalate hemihydrate $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ (Mutin et al., 1981) has been studied by single-crystal X-ray diffraction analysis. Hydrogen bonds were not investigated. Two modifications of the anhydrous compound $\mathrm{BaC}_{2} \mathrm{O}_{4}$ (Walter-Levy \& Laniepce, 1965) have been reported. The present study was made to complete the description of hydrogen bonding in barium oxalates and to characterize anhydrous barium oxalate.

## 2. Experimental

### 2.1. Chemistry

Barium chloride, $\mathrm{BaCl}_{2} \cdot 2 \mathrm{H}_{2} \mathrm{O}$ (Merck p.a.), and ammonium oxalate, $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{C}_{2} \mathrm{O}_{4} \cdot \mathrm{H}_{2} \mathrm{O}$ (Merck p.a.), were used in the synthesis. $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ was obtained when 500 ml of a 0.2 M solution of $\mathrm{BaCl}_{2} \cdot 2 \mathrm{H}_{2} \mathrm{O}$ was added dropwise at room temperature to 500 ml of a 0.2 M solution of $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{C}_{2} \mathrm{O}_{4} \cdot \mathrm{H}_{2} \mathrm{O}$. The white crystalline product of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ was washed with water, filtered and dried at room temperature. The deuterated compound $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{D}_{2} \mathrm{O}$ was made in a similar way using $99.99 \% \mathrm{D}_{2} \mathrm{O}$ (Norsk Hydro) as the solvent.

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Recrystallization and crystal growth of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ was investigated by hydrothermal synthesis in the temperature range $403-498 \mathrm{~K}$. Approximately 7 g of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ was heated with 175 ml water for 80 h . The reaction product was $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$. The hydrothermal treatments did not improve the crystal quality and size of the crystals. Hydrothermal synthesis made at 593 K resulted in the formation of $\mathrm{BaCO}_{3}$. Larger crystals of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ were made by slow mixing of a barium chloride and an ammonium oxalate solution in a diffusion mode, as described elsewhere (Christensen et al., 1991).

Differential thermal analysis and thermogravimetric analysis of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ were performed in the temperature range $293-746 \mathrm{~K}$ using a Stanton Redcroft TG-DTA simultaneous thermal analyzer STA 1000/1500 using a heating rate of $5 \mathrm{~K} \mathrm{~min}^{-1}$ and Ar gas flow on the sample. The dehydration to $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ takes place in the temperature interval $383-418 \mathrm{~K}$ and the loss in weight of $3.0 \%$ corresponds to the formation of the anhydrous compound, see Fig. 1 (calculated value $3.8 \%$ ). A phase transition from $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ to $\beta-\mathrm{BaC}_{2} \mathrm{O}_{4}$ was reported to take place at approximately 663 K (WalterLevy \& Laniepce, 1965) and $\beta-\mathrm{BaC}_{2} \mathrm{O}_{4}$ was only stable in a narrow temperature range before the compound decomposed to $\mathrm{BaCO}_{3}$. The heating was interrupted, see Fig. 1, when $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ started to lose weight and an X-ray powder pattern of the sample had reflections of $\beta-\mathrm{BaC}_{2} \mathrm{O}_{4}, \alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ and $\mathrm{BaCO}_{3}$.

The thermal decomposition of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{D}_{2} \mathrm{O}$ was also investigated in the temperature range $373-753 \mathrm{~K}$ in gravimetric analyses where samples of the compound placed in Pt crucibles were heated in an electric furnace for up to 15 h . The temperature in the furnace was measured with a Pt-Pt $13 \%$ Rh thermocouple. The loss in weight in the temperature range $633-753 \mathrm{~K}$ is displayed in Fig. 2. The sample was only dried at room temperature and the observed loss in weight exceeds the loss of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{D}_{2} \mathrm{O}$ to $\mathrm{BaCO}_{3}$, which is $16.2 \%$. Powder patterns were taken of the samples after the heat treatments to identify the decomposition products (see below) and had reflections of $\beta-\mathrm{BaC}_{2} \mathrm{O}_{4}, \alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ and $\mathrm{BaCO}_{3}$.


Figure 1
DTA and TGA diagrams for the dehydration of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ to $\alpha$ $\mathrm{BaC}_{2} \mathrm{O}_{4}$. The dehydration takes place in the temperature interval 383418 K.

The IR spectrum of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ was measured on a Perkin-Elmer Paragon 1000 FT-IR spectrometer. An absorption at $3500 \mathrm{~cm}^{-1}$ indicates that there are no strong hydrogen bonds with short bond distances in the structure.

### 2.2. X-ray and neutron powder diffraction

The purity of the synthesized products was tested with X-ray diffraction powder patterns measured on a Stoe-Stadi powder diffractometer using $\mathrm{Cu} K \alpha_{1}$ radiation ( $\lambda=1.5406 \AA$ ). A transmission mode was applied with a flat sample on tape. The diffractometer was calibrated with an external silicon standard $\left(a_{\text {Si }}=5.43050 \AA\right)$. The counter was a curved positionsensitive detector covering $40^{\circ}$ in $2 \theta$ or a linear detector covering $5^{\circ}$ in $2 \theta$ and used in a step scan mode. The X-ray powder patterns of the samples used in the thermal decomposition of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{D}_{2} \mathrm{O}$ were measured on a Philips diffractometer using Co $K \alpha_{1}(\lambda=1.7889 \AA$ ).

Synchrotron X-ray powder diffraction patterns of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ were measured on the powder diffractometer at the beamline X7A at NSLS, Brookhaven National Laboratory. The sample was kept in a 0.2 mm -diameter quartz glass capillary, which was rotated at 50 r.p.m. to randomize the crystallites. A neutron diffraction powder pattern of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{D}_{2} \mathrm{O}$ was measured at the diffractometer D 1 A at the Institute Max von Laue-Paul Langevin. The experimental data for the measured powder patterns are listed in Table 1.

### 2.3. In situ study of the $\mathrm{BaC}_{\mathbf{2}} \mathrm{O}_{\mathbf{4}} \cdot \mathbf{0} \cdot \mathbf{5} \mathrm{H}_{\mathbf{2}} \mathrm{O}$ decomposition

The decomposition of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ to $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ was investigated by time-resolved X-ray powder diffraction using an INEL diffractometer with a position-sensitive detector


Figure 2
Loss in weight of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{D}_{2} \mathrm{O}$ versus temperature. Ex situ investigations. Each point represents a sample kept at the temperature for 8-12 h.

Table 1
Experimental data for the measured powder patterns of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ (I), $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{D}_{2} \mathrm{O}$ (II) and $\mathrm{BaC}_{2} \mathrm{O}_{4}$ (III).

| Sample | (I) | (I) | (I) | (II) | (III) | (III) | (III) | (III) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Powder pattern | A | B | C | D | E | F | G | H |
| Diffractometer | Stoe-Stadi | INEL CSIRO | X7A NSLS | D1A ILL | Stoe-Stadi | Philips CSIRO | INEL CSIRO | Philips |
| Radiation | $\mathrm{Cu} K \alpha_{1}$ | $\mathrm{Cu} K \alpha_{1,2}$ | Synchrotron | Neutron | $\mathrm{Cu} K \alpha_{1}$ | $\mathrm{Cu} K \alpha_{1,2}$ | $\mathrm{Cu} K \alpha_{1,2}$ | $\mathrm{Cu} K \alpha_{1}$ |
| $2 \theta_{\text {min }}\left({ }^{\circ}\right.$ ) | 1.00 | 1.00 | 8.00 | 12.00 | 10.00 | 8.00 | 1.00 | 8.00 |
| $2 \theta_{\text {max }}\left({ }^{\circ}\right.$ ) | 70.00 | 121.00 | 74.00 | 152.00 | 70.00 | 50.00 | 121.00 | 58.00 |
| $\Delta 2 \theta\left({ }^{\circ}\right)$ | 0.02 | 0.03 | 0.01 | 0.05 | 0.02 | 0.02 | 0.03 | 0.02 |
| $\lambda(\mathrm{A})$ | 1.5406 | 1.5418 | 1.3150 | 1.9090 | 1.5406 | 1.5418 | 1.5418 | 1.7889 |
| Max $\sin \theta / \lambda\left(\AA^{-1}\right)$ | 0.472 | 0.564 | 0.458 | 0.508 | 0.372 | 0.274 | 0.564 | 0.271 |
| Flat plate | Yes | Yes |  |  | Yes | Yes | Yes | Yes |
| Capillary 0.2 mm |  |  | Yes |  |  |  |  |  |
| V container |  |  |  | Yes |  |  |  |  |
| Diameter (cm) |  |  |  | 12 |  |  |  |  |
| Rotation of sample (r.p.m.) | 60 |  | 60 |  | 60 |  |  |  |
| Temperature (K) | 298 | 298 | 298 | 298 | 298 | 473 | 393 | 298 |

Table 2
Experimental data and unit-cell parameters for the low-temperature single-crystal measurement of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$.

| $a(\AA)$ | $8.692(1)$ |
| :--- | :--- |
| $b(\AA)$ | $9.216(1)$ |
| $c(\AA)$ | $6.146(1)$ |
| $\alpha\left({ }^{\circ}\right)$ | $95.094(3)$ |
| $\beta\left({ }^{\circ}\right)$ | $95.492(3)$ |
| $\gamma\left({ }^{\circ}\right)$ | $64.500(3)$ |
| Cell volume $\left(\AA^{3}\right)$ | 441.7 |
| Space group | $P \overline{1}$ |
| $Z$ | 4 |
| Density (calc) $\left(\mathrm{g} \mathrm{cm}^{-3}\right)$ | 3.45 |
| Size of crystal $(\mathrm{mm})$ | $0.01 \times 0.06 \times 0.15$ |
| Linear absorption coefficient, $\mu\left(\mathrm{mm}^{-1}\right)$ | 9.0 |
| No. of measured reflections | 6475 |
| No. of independent reflections with $I>3 \sigma(I)$ | 1339 |
| $R(F)$ | 0.049 |
| $T(\mathrm{~K})$ | 120 |

covering a $2 \theta$ range of $120^{\circ}$ and with a Philips X'Pert diffractometer using a step scan mode. The flat sample holder on each of the diffractometers was a platinum plate which was also the heating element, controlled by an Anton Paar HTK2HC temperature controller. A $\mathrm{Pt}-\mathrm{Pt} 10 \% \mathrm{Rh}$ thermocouple was welded to the back of the sample holder. The powder samples were mixed with acetone and the mixture was placed on the sample holder with a pipette. The powder sample proved to have excellent contact with the sample holder, resulting in only a small temperature gradient between sample, heater (sample holder) and thermocouple. The


Figure 3
Stereoscopic view of the structure of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ along [001].
samples were housed in a vacuum chamber with Mylar windows at a pressure of approximately 10 torr. The diffractometers were calibrated with an external standard of $\mathrm{Y}_{2} \mathrm{O}_{3}$ and temperature calibration was made with a sample of $\mathrm{KNO}_{3}$, which showed the $\alpha-\beta$ transition of the compound on heating at 403 K . This is in acceptable agreement with the reported transition temperatures 401 and 402 K , respectively (Christensen et al., 1996; Weast et al., 1987). At this pressure the decomposition temperature of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ to $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ was 370 (3) K. The magnitude of the temperature gradient of the sample exposed by the X-ray beam is not known.

### 2.4. X-ray single-crystal diffraction of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot \mathbf{0 . 5} \mathrm{H}_{2} \mathrm{O}$

Single-crystal diffraction data were measured at 120 K on a Siemens SMART diffractometer with an area detector, using Mo $K \alpha$ radiation $(\lambda=0.7107 \AA)$. Experimental and crystallographic data are listed in Table 2. ${ }^{1}$ The direct-method program SIR (Altomare et al., 1994) gave the positions of all the atoms in the structure of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ and a final Fourier map did not show any additional electron density. The structure was refined with the least-squares program LINUS (LINUS is the 1971 version of ORFLS; Busing et al., 1962) with scattering contributions from neutral atoms (Cromer \& Waber, 1964) and corrections for anomalous scattering contributions for the Ba atom (MacGillavry et al., 1962). Absorption corrections were applied (Busing et al., 1962). Atomic coordinates and thermal displacement parameters are given in Table 3 and some interatomic distances are given in Table 4. A stereoscopic view of the structure along [001] with the $a$ axis across the page is displayed in Fig. 3.

## 3. Analysis of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot \mathbf{0 . 5} \mathrm{H}_{2} \mathrm{O}$ single-crystal diffraction data

The two Ba atoms are coordinated to nine O atoms with bonds from 2.73 (1) to $2.99(1) \AA$, and 2.73 (1) to $2.91(1) \AA$,

[^0]Table 3
Positional parameters for the structure of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O} / \mathrm{D}_{2} \mathrm{O}$.
For each atom are listed: first line: refined parameters from X-ray singlecrystal data; second line: EXPO solution from pattern C; third line: EXPO solution from pattern D ; fourth line: refined parameters neutron diffraction powder pattern D .

|  | $x$ | $y$ | $z$ |
| :---: | :---: | :---: | :---: |
| Ba1 | 0.9558 (1) | 0.2093 (1) | 0.2782 (1) |
|  | 0.964 | 0.207 | 0.284 |
|  | - | - | - |
|  | 0.965 (2) | 0.206 (2) | 0.273 (3) |
| Ba2 | 0.3635 (1) | 0.4185 (1) | 0.2132 (1) |
|  | 0.367 | 0.415 | 0.207 |
|  | - | - | - |
|  | 0.369 (2) | 0.422 (2) | 0.206 (3) |
| C1 | 0.923 (2) | 0.676 (2) | 0.176 (3) |
|  | 0.869 | 0.675 | 0.127 |
|  | 0.906 | 0.623 | 0.152 |
|  | 0.908 (2) | 0.662 (2) | 0.190 (3) |
| C2 | 0.819 (2) | 0.626 (2) | 0.324 (3) |
|  | 0.840 | 0.638 | 0.340 |
|  | 0.834 | 0.663 | 0.335 |
|  | 0.815 (2) | 0.632 (2) | 0.313 (3) |
| O1 | 0.874 (1) | 0.686 (1) | -0.020 (2) |
|  | 0.900 | 0.676 | -0.001 |
|  | 0.864 | 0.708 | 0.006 |
|  | 0.881 (3) | 0.683 (3) | -0.026 (3) |
| O 2 | 1.048 (1) | 0.696 (1) | 0.267 (2) |
|  | 1.031 | 0.765 | 0.314 |
|  | 1.029 | 0.757 | 0.293 |
|  | 1.052 (2) | 0.693 (2) | 0.269 (3) |
| O3 | 0.747 (1) | 0.540 (1) | 0.239 (2) |
|  | 0.745 | 0.559 | 0.275 |
|  | 0.784 | 0.554 | 0.256 |
|  | 0.736 (2) | 0.546 (2) | 0.244 (3) |
| O4 | 0.818 (2) | 0.673 (1) | 0.525 (2) |
|  | 0.797 | 0.672 | 0.527 |
|  | 0.767 | 0.670 | 0.404 |
|  | 0.813 (2) | 0.670 (2) | 0.534 (3) |
| C3 | 0.276 (2) | 0.821 (2) | 0.135 (2) |
|  | 0.309 | 0.797 | 0.175 |
|  | 0.309 | 0.833 | 0.082 |
|  | 0.276 (2) | 0.818 (2) | 0.133 (3) |
| C4 | 0.287 (2) | 0.816 (2) | 0.385 (3) |
|  | - | - | - |
|  | 0.334 | 0.805 | 0.327 |
|  | 0.279 (2) | 0.812 (2) | 0.390 (3) |
| O5 | 0.356 (1) | 0.690 (1) | 0.028 (2) |
|  | 0.335 | 0.688 | 0.062 |
|  | 0.372 | 0.734 | -0.028 |
|  | 0.360 (2) | 0.683 (2) | 0.020 (2) |
| O6 | 0.185 (1) | 0.950 (1) | 0.050 (2) |
|  | 0.184 | 0.936 | 0.027 |
|  | 0.216 | 0.959 | 0.027 |
|  | 0.181 (3) | 0.953 (2) | 0.030 (3) |
| O7 | 0.370 (1) | 0.685 (1) | 0.474 (2) |
|  | 0.359 | 0.694 | 0.478 |
|  | - | - | - |
|  | 0.369 (2) | 0.678 (2) | 0.478 (3) |
| O8 | 0.199 (1) | 0.947 (1) | 0.487 (2) |
|  | 0.215 | 0.911 | 0.481 |
|  | - | - | - |
|  | 0.204 (2) | 0.946 (2) | 0.485 (3) |
| O9 | 0.516 (2) | 0.070 (1) | 0.221 (2) |
|  | 0.548 | 0.054 | 0.193 |
|  | 0.438 | 0.091 | 0.287 |
|  | 0.500 (3) | 0.082 (3) | 0.210 (4) |
| H1 | 0.58 | 0.04 | 0.24 |
|  | - | - | - |
|  | - | - | - |
|  | 0.615 (5) | 0.035 (5) | 0.282 (6) |
| H2 | 0.45 | 0.08 | 0.15 |
|  | - | - | - |

Table 3 (continued)

|  | $x$ | $y$ | $z$ |
| :--- | :--- | :--- | :--- |
|  | - | - | - |
| $\mathrm{H}^{\prime}$ | $0.488(6)$ | $0.076(6)$ | $0.110(5)$ |
|  | - | - | - |
|  | - | - | - |
|  | - | $0.104(5)$ | - |
|  | $0.409(5)$ | $0.315(8)$ |  |

respectively, and in deformed prisms similar to the coordination polyhedra in the structures of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 3.5 \mathrm{D}_{2} \mathrm{O}$ (Neder et al., 1997). One of the two oxalate ions deviates significantly from planarity. The distances to the best plane through the six atoms of the oxalate ion containing the atoms $\mathrm{C} 1, \mathrm{C} 2$ and $\mathrm{O} 1-$ O 4 are: $\mathrm{C} 1-0.02, \mathrm{C} 2-0.01, \mathrm{O} 1-0.27, \mathrm{O} 20.28, \mathrm{O} 30.28, \mathrm{O} 4$ $-0.27 \AA$. The deviation from planarity of this oxalate ion is thus significant. The distances to the best plane through the atoms of the oxalate ion containing the atoms $\mathrm{C} 3, \mathrm{C} 4$ and $\mathrm{O} 5-$ O8 are: C3 $-0.02, \mathrm{C} 4-0.03$, O5 0.01 , O6 0.02 , O7 $0.02, \mathrm{O} 8$ $0.01 \AA$. The deviation from planarity of this oxalate ion is marginal. The water molecule with the atoms O9, H1 and H2 does take part in a hydrogen bond where the bond distance $\mathrm{O} 9-\mathrm{O} 8$ is $2.88(2) \AA$.

## 4. Analysis of powder diffraction patterns

## 4.1. $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot \mathbf{0 . 5} \mathrm{H}_{2} \mathrm{O}$ : test of structure solution from X-ray powder diffraction data

Unit-cell parameters and space groups for the barium oxalate hydrates and the anhydrous barium oxalate are listed in Table 5. The X-ray diffraction powder pattern of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$, Table 1, C, was indexed with the program FZON (Visser, 1969) on a triclinic cell. This cell is different from that of Mutin et al. (1981), but that unit cell can be converted to the unit cell of this work by the matrix

$$
\begin{array}{ccc}
-1 & -1 & 0 \\
-1 & 0 & 0 \\
0 & 0 & -1
\end{array}
$$

and this is also the cell used on the ICDD card No. 20-134 and in the single-crystal structure analysis above. The powder pattern was decomposed by the program $A L L H K L$ (Pawley, 1981) giving an $R$ value of 0.091 for each of the two unit cells. A structure solution was obtained using the direct-method program EXPO (Altomare et al., 1995). The results of the structure solution are given in Table 3. The two Ba atoms were found in excellent agreement with the results of the singlecrystal data analysis and only three atoms, C4, H1 and H2, could not be located. A synchrotron X-ray powder diffraction pattern can thus give an almost complete crystal structure even in the case of a heavy-atom structure.

## 4.2. $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{D}_{2} \mathrm{O}$ : structure solution from neutron diffraction powder data

The average scattering contribution from the $\mathrm{Ba}, \mathrm{C}, \mathrm{O}$ and D atoms are in the neutron diffraction case 8.8, 28.5, 48.9 and

Table 4
Interatomic distances (in $\AA$ ) of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$.
X-ray single-crystal data and positional parameters for H atoms from profile refinement of neutron powder diffraction data. Symmetry operations give positions of the O atoms with reference to the positions listed in Table 4.

| Ba1-O6 ${ }^{\text {i }}$ | 2.73 (1) | $\mathrm{Ba} 2-\mathrm{O} 5^{\mathrm{ii}}$ | 2.73 (1) |
| :---: | :---: | :---: | :---: |
| $\mathrm{Ba} 1-\mathrm{O} 1^{\text {iii }}$ | 2.75 (1) | $\mathrm{Ba} 2-\mathrm{O} 7^{\text {iv }}$ | 2.75 (1) |
| $\mathrm{Ba} 1-\mathrm{O}^{\mathrm{i}}$ | 2.76 (1) | $\mathrm{Ba} 2-\mathrm{O} 1^{\mathrm{ii}}$ | 2.76 (1) |
| $\mathrm{Ba} 1-\mathrm{O} 4^{\text {v }}$ | 2.77 (1) | $\mathrm{Ba} 2-\mathrm{O} 4^{\text {iv }}$ | 2.77 (1) |
| $\mathrm{Ba} 1-\mathrm{O} 3$ | 2.82 (1) | $\mathrm{Ba} 2-\mathrm{O} 5$ | 2.81 (1) |
| $\mathrm{Ba} 1-\mathrm{O} 2^{\text {v }}$ | 2.85 (1) | $\mathrm{Ba} 2-\mathrm{O} 7$ | 2.83 (1) |
| $\mathrm{Ba} 1-\mathrm{O} 6^{\text {ii }}$ | 2.88 (1) | $\mathrm{Ba} 2-\mathrm{O} 2^{\text {vi }}$ | 2.85 (1) |
| $\mathrm{Ba} 1-\mathrm{O} 8^{\text {iv }}$ | 2.90 (1) | $\mathrm{Ba} 2-\mathrm{O} 3{ }^{\text {ii }}$ | 2.86 (1) |
| $\mathrm{Ba} 1-\mathrm{O} 5^{\mathrm{ii}}$ | 2.99 (1) | Ba2-O9 | 2.91 (1) |
| C1-O1 | 1.24 (2) | C3-O5 | 1.26 (2) |
| $\mathrm{C} 1-\mathrm{O} 2$ | 1.25 (2) | C3-O6 | 1.25 (2) |
| C2-O3 | 1.25 (2) | C4-O7 | 1.25 (2) |
| C2-O4 | 1.27 (2) | C4-O8 | 1.27 (2) |
| C1-C2 | 1.56 (2) | C3-C4 | 1.53 (2) |
| O9-H1 | 0.70 (11) |  |  |
| O9-H2 | 0.95 (15) |  |  |
| $\mathrm{O} 9-\mathrm{O} 8^{\text {iv }}$ | 2.88 (2) (hydrogen bond) |  |  |
| O9-O9 | 2.90 (3) |  |  |

Symmetry codes: (i) $1+x, y-1, z$; (ii) $2-x, 1-y,-z$; (iii) $2-x, 1-y, 1-z$; (iv) $1-x$, $1-y,-z$; (v) $1-x, 1-y, 1-z$; (vi) $x-1, y, z$.
$13.8 \%$, respectively. The neutron diffraction powder pattern, Table 1, D, was used with the direct method program EXPO (Altomare et al., 1995) in a structure solution and the results are given in Table 3. The atoms Ba1, Ba2, O7, O8, H1(D1) and $\mathrm{H} 2(\mathrm{D} 2)$ were not found. The initial positions of the D atoms of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{D}_{2} \mathrm{O}$ were derived from the single-crystal investigation and the model of the structure was refined using the least-squares program $D B W 3.2 S$ (Wiles et al., 1988). Positional parameters are given in Table 3 and are in acceptable agreement with the positional parameters found in the single-crystal X-ray diffraction analysis. The water molecule forms weak hydrogen bonds in the structure. The atom H1(D1) is part of the $\mathrm{O} 9-\mathrm{O} 8$ hydrogen bond of 2.88 (2) $\AA$. The $\mathrm{O} 9-\mathrm{O} 9$ distance over a center of symmetry of 2.90 ( 3 ) $\AA$ indicates that the H atom of the water molecule H 2 (D2) must be placed statistically in two sites, as indicated in Table 3.

## 4.3. $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$

The solid-state decomposition of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ to $\mathrm{BaC}_{2} \mathrm{O}_{4}$ results readily in the formation of the $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ modification, but the $\beta-\mathrm{BaC}_{2} \mathrm{O}_{4}$ modification may also be obtained. $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ can absorb water so that $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ is formed. It is thus a challenge to make a pure sample of $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ and $\beta-\mathrm{BaC}_{2} \mathrm{O}_{4}$ and powder patterns of $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ stored for a few days often show $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ as an impurity. The patterns, Table 1, G and F, were recorded in the in situ experiments with the INEL and Philips diffractometers and gave patterns of $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ without $\beta-\mathrm{BaC}_{2} \mathrm{O}_{4}$ and $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ as impurities.

Assuming a linear relation of the volume of one formula unit of the barium oxalate hydrates $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot x \mathrm{H}_{2} \mathrm{O}$ versus $x$ ( $x=\frac{1}{2}, 1,2$ and 3.5), the volume of one formula unit of $\mathrm{BaC}_{2} \mathrm{O}_{4}$ would be approximately $100 \AA^{3}$. The powder pattern, Table 1 , F , of $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ was indexed with the program DICVOL
(Boultif \& Louër, 1991) on a triclinic cell with a volume of $393 \AA^{3}$, in agreement with the expected volume of four $\mathrm{BaC}_{2} \mathrm{O}_{4}$ formula units.

Pattern F was decomposed by the program ALLHKL (Pawley, 1981) giving an $R$ value of $7.0 \%$. The indexed powder pattern of $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ is listed in Table 6. The reflection with $d=$ $2.715 \AA$ is in different patterns observed with different intensities and is possibly due to an impurity. With this reflection omitted pattern F could also be decomposed with ALLHKL (Pawley, 1981), giving an $R$ value of 0.073 and a unit cell with half the volume of that reported above. This corresponds to four or two formula units of $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ in the two cells, respectively. The indexed powder pattern, Table 6 , has almost all reflection with $l=2 n$, and the first observed lowangle reflection of $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ is at $d=5.014 \AA$, in contrast to the first observed low-angle reflection of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ at $d=8.360 \AA$. This could support the hypothesis that the unitcell volume of $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ was half that of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ and thus has a volume of $197 \AA^{3}$ with the unit-cell parameters $a=5.137$ (3), $b=8.764$ (7), $c=4.503$ (5) $\AA, \alpha=83.57$ (4), $\beta=98.68$ (5), $\gamma=99.53(5)^{\circ}$. The two cells were used in attempts to solve the structure of $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ from the X-ray



Figure 4
Powder patterns of samples kept at 633 and 718 K , respectively. Reflections marked with arrows are from $\beta-\mathrm{BaC}_{2} \mathrm{O}_{4}$. Other reflections are from $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ ( 633 K pattern) and from $\mathrm{BaCO}_{3}$ ( 718 K pattern).

Table 5
Unit-cell parameters and space groups for the barium oxalate hydrates and for anhydrous barium oxalate.
Powder pattern: the capital letters refer to the patterns listed in Table 2.

|  | $a$ | $b$ | $c$ | $\alpha$ | $\beta$ | $\gamma$ | Space group | Ref./ICDD | Powder pattern |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 3.5 \mathrm{D}_{2} \mathrm{O}$ | 13.489 (1) | 7.663 (19) | 15.085 (1) |  | 113.57 (1) |  | C2/c | 1 |  |
| $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 2 \mathrm{D}_{2} \mathrm{O}$ | 7.538 (1) | 11.062 (1) | 7.105 (1) |  | 105.42 (1) |  | $P 2_{1} / \mathrm{c}$ | 2 |  |
| $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot \mathrm{D}_{2} \mathrm{O}$ | 10.0648 (3) | 7.9350 (2) | 6.8503 (2) |  | 122.35 (2) |  | C2/m | 3 |  |
| $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{D}_{2} \mathrm{O}$ | 9.312 (1) | 9.649 (1) | 6.188 (1) | 90.13 (2) | 95.36 (2) | 125.18 (2) | $P \overline{1}$ | 4 |  |
| $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{D}_{2} \mathrm{O}$ | 8.748 | 9.298 | 6.170 | 94.91 | 95.48 | 64.19 | $P 1$ | 20-134 |  |
| $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{D}_{2} \mathrm{O}$ | 8.751 (1) | 9.308 (1) | 6.172 (1) | 94.98 (1) | 95.51 (1) | 64.16 (1) | $P 1$ | This work | C |
| $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{D}_{2} \mathrm{O}$ | 8.684 (2) | 9.241 (2) | 6.153 (2) | 95.55 (2) | 95.53 (2) | 64.43 (2) | $P 1$ | This work | D $\dagger$ |
| $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ | 5.137 (3) | 8.764 (6) | 9.006 (4) | 83.57 (4) | 98.68 (5) | 99.53 (5) | $P 1$ | This work | F |
| $\beta-\mathrm{BaC}_{2} \mathrm{O}_{4}$ | 8.71 (2) | 6.99 (2) | 9.91 (3) | 89.4 (2) | 96.0 (2) | 92.9 (2) | $P 1$ | 19-125 |  |

 $0.5 \%$.

Table 6
Indexed powder pattern of $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$.
The observed intensities derived in a profile fit to the pattern using the program ALLHKL (Pawley, 1981).

| $2 \theta_{\text {obs }}\left({ }^{\circ}\right)$ | $2 \theta_{\text {calc }}\left({ }^{\circ}\right.$ ) | $d_{\text {obs }}(\AA)$ | $d_{\text {calc }}(\AA)$ | $I_{\text {obs }}$ | $h k l$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 17.67 | 17.65 | 5.014 | 5.020 | 47 | 100 |
| 19.07 | 19.09 | 4.651 | 4.646 | 4 | 101 |
|  | 19.06 |  | 4.654 |  | 110 |
| 19.97 | 19.93 | 4.443 | 4.451 | 15 | 111 |
|  | 20.01 |  | 4.434 |  | 002 |
| 20.60 | 20.62 | 4.307 | 4.304 | 53 | 020 |
| 21.68 | 21.69 | 4.095 | 4.093 | 52 | 012 |
| 23.33 | 23.36 | 3.810 | 3.806 | 20 | 012 |
| 24.89 | 24.91 | 3.575 | 3.571 | 85 | 102 |
| 25.11 | 25.11 | 3.543 | 3.543 | 100 | 120 |
| 27.54 | 27.54 | 3.236 | 3.236 | 29 | 022 |
| 28.66 | 28.64 | 3.112 | 3.114 | 23 | 121 |
| 29.29 | 29.28 | 3.047 | 3.048 | 23 | 120 |
| 30.16 | 30.13 | 2.961 | 2.964 | 7 | 112 |
|  | 30.18 |  | 2.959 |  | $02 \overline{2}$ |
| 30.77 | 30.76 | 2.903 | 2.905 | 23 | 112 |
| 32.96 | 32.93 | 2.715 | 2.718 | 8 | 113 |
| 34.98 | 34.96 | 2.563 | 2.565 | 6 | $12 \overline{2}$ |
| 35.40 | 35.40 | 2.533 | 2.534 | 38 | $12 \overline{2}$ |
| 36.03 | 36.04 | 2.491 | 2.490 | 8 | 122 |
| 38.17 | 38.17 | 2.356 | 2.356 | 4 | 212 |
| 38.63 | 38.67 | 2.329 | 2.327 | 45 | 220 |
| 38.86 | 38.85 | 2.316 | 2.316 | 15 | 032 |
|  | 38.83 |  | 2.317 |  | 210 |
| 40.51 | 40.50 | 2.225 | 2.225 | 2 | $22 \overline{2}$ |
| 41.09 | 41.10 | 2.195 | 2.195 | 3 | 014 |
| 41.83 | 41.84 | 2.158 | 2.158 | 17 | 033 |
| 42.07 | 42.07 | 2.146 | 2.146 | 14 | $1 \overline{3} 2$ |
| 43.00 | 43.00 | 2.102 | 2.102 | 16 | 123 |
|  | 43.00 |  | 2.102 |  | 014 |
|  | 43.00 |  | 2.102 |  | 123 |

Triclinic cell $a=5.137$ (3), $b=8.714$ (6), $c=9.006$ (4) $\AA, \alpha=83.57$ (4), $\beta=98.68$ (5), $\gamma=$ $99.53(5)^{\circ}, M(25)=12.6$.
powder patterns. The program $E X P O$ (Altomare et al., 1995) was used and yielded solutions with positions of the heavy Ba atoms. None of these could give calculated intensities of the models in sufficient agreement with the observed intensities, using the powder patterns Table 1, F and H. These patterns had much higher intensities of the observed reflections in the $2 \theta$ ranges 24.5-25.3 (pattern F) and 28.0-30.0 (pattern H) than the calculated intensities from the models. The powder patterns available were thus not sufficiently resolved.

Synchrotron X-ray diffraction patterns would be necessary for a solution of the structure of $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$.

## 4.4. $\boldsymbol{\beta}-\mathrm{BaC}_{2} \mathrm{O}_{4}$

In the synthesis of barium oxalate from $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{D}_{2} \mathrm{O}, \beta-\mathrm{BaC}_{2} \mathrm{O}_{4}$ was only obtained as an impurity phase. Samples of $\mathrm{BaC}_{2} \mathrm{O}_{4} \cdot 0.5 \mathrm{D}_{2} \mathrm{O}$ kept in the temperature range $633-718 \mathrm{~K}$ (Fig. 2) had reflections of $\beta-\mathrm{BaC}_{2} \mathrm{O}_{4}, \alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ and $\mathrm{BaCO}_{3}$ in their powder patterns. Fig. 4 displays a $2 \theta$ range of the powder pattern of two samples kept at 633 and 718 K , respectively. The pattern of the sample kept at 633 K has strong reflections of $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ and reflections of $\beta$ - $\mathrm{BaC}_{2} \mathrm{O}_{4}$ marked with arrows and $d$-spacing values which are in agreement with the values listed for $\beta-\mathrm{BaC}_{2} \mathrm{O}_{4}$ in the ICDD database card No. 19-125. The pattern of the sample kept at 718 K has strong reflections of $\mathrm{BaCO}_{3}$ and also reflections of $\beta-\mathrm{BaC}_{2} \mathrm{O}_{4}$. The compound $\beta-\mathrm{BaC}_{2} \mathrm{O}_{4}$ can thus coexist both with $\alpha-\mathrm{BaC}_{2} \mathrm{O}_{4}$ and with $\mathrm{BaCO}_{3}$, and it is formed in a temperature range where the loss in weight of barium oxalate is increasing (Fig. 2). The strong $\beta-\mathrm{BaC}_{2} \mathrm{O}_{4}$ reflection at $d=3.72 \AA$ has the same position as the strong reflection of $\mathrm{BaCO}_{3}$ at $3.722 \AA$.

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[^0]:    ${ }^{\mathbf{1}}$ Supplementary data for this paper are available from the IUCr electronic archives (Reference: OS0083). Services for accessing these data are described at the back of the journal.

